

Metabolic Flux Analysis: Understanding and Applications in Biotechnology

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Abstract

Metabolic flux analysis (MFA) is a powerful tool used to quantify the flow of metabolites through metabolic pathways. This paper aims to explore the principles, methodologies, and applications of MFA in biotechnology. By integrating data from various sources and applying computational models, MFA provides insights into cellular metabolism, aiding in the optimization of industrial processes, the development of therapeutic strategies, and the enhancement of our understanding of metabolic diseases.

Keywords: Metabolic Flux Analysis, Biotechnology, Metabolic Pathways, Isotope Labeling, Mass Spectrometry, NMR Spectroscopy, Computational Modeling.

1. Introduction

Metabolic Flux Analysis (MFA) has emerged as a fundamental technique in the field of biotechnology, offering profound insights into the metabolic processes of living organisms. At its core, MFA quantifies the rates at which metabolites are produced, consumed, and transformed within a cell, providing a detailed map of cellular metabolic activity[1]. This analysis is crucial for understanding the complex network of biochemical reactions that sustain life and for identifying key control points within these networks. The ability to map these fluxes with precision allows researchers to manipulate metabolic pathways for various applications, ranging from industrial bioprocessing to medical therapeutics.

The development and application of MFA have been significantly propelled by advances in experimental techniques and computational modeling. Isotopic

labeling and mass spectrometry have enabled the accurate measurement of intracellular metabolites, while sophisticated algorithms such as Flux Balance Analysis (FBA) have allowed for the precise calculation of metabolic fluxes[2]. These tools have collectively transformed MFA from a theoretical concept into a practical methodology that can be applied to real-world biological systems. By leveraging these technologies, researchers can construct comprehensive stoichiometric models that serve as blueprints for cellular metabolism.

One of the primary motivations behind the use of MFA in biotechnology is its potential to optimize microbial production systems. Microorganisms such as bacteria and yeast are often employed as cell factories for the production of valuable compounds, including biofuels, pharmaceuticals, and industrial chemicals. Through MFA, scientists can identify metabolic bottlenecks and inefficiencies within these production pathways and implement targeted genetic modifications to enhance yield and productivity. This approach not only improves the economic viability of bioprocesses but also contributes to the development of more sustainable and eco-friendly production methods.

Beyond its industrial applications, MFA plays a critical role in advancing our understanding of disease mechanisms and developing novel therapeutic strategies. In the realm of drug development, MFA can reveal how drug candidates affect cellular metabolism, uncovering potential side effects and off-target interactions[3]. Additionally, MFA is instrumental in studying the altered metabolic states of cancer cells, enabling the identification of unique metabolic dependencies that can be targeted for cancer treatment. As such, MFA is a versatile tool that bridges the gap between basic metabolic research and applied biotechnology, offering a pathway to innovations in both health and industry.

2. Principles of Metabolic Flux Analysis

Metabolic Flux Analysis (MFA) is fundamentally based on the principle of mass balance within a cellular system. At its core, MFA involves the construction of a stoichiometric model that represents the metabolic network of a cell. This model is a set of linear equations where each equation corresponds to a metabolic reaction, linking substrates and products. The stoichiometric coefficients in these equations represent the number of molecules involved in each reaction. By applying the principle of mass conservation, the total influx and efflux of metabolites in the system are balanced, providing a framework for analyzing the flow of metabolites through the network[4].

A critical component of MFA is the accurate measurement of metabolite concentrations and reaction rates. Experimental techniques such as isotopic labeling and tracer studies are employed to track the flow of metabolites within the cell. Isotopic labeling involves incorporating a detectable isotope, such as ^{13}C , into metabolic substrates. As the labeled substrate is metabolized, the isotope is distributed through various metabolic intermediates, which can be quantified using analytical techniques like mass spectrometry (MS) and nuclear magnetic resonance (NMR) spectroscopy[5]. These measurements provide essential data for calculating the fluxes of metabolic reactions. The fig.1 depicts Principles of Metabolic Flux Analysis.

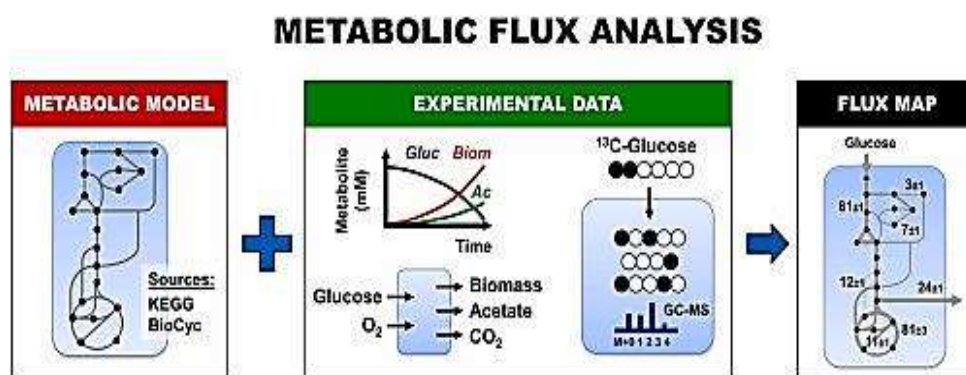


Fig.1 Principles of Metabolic Flux Analysis

Once experimental data is collected, computational methods are applied to estimate the metabolic fluxes. Flux Balance Analysis (FBA) is a widely used computational approach in MFA. FBA utilizes linear programming to solve the system of stoichiometric equations under the assumption of steady-state conditions, where the concentrations of metabolites remain constant over time. This method identifies the optimal distribution of fluxes that satisfies the mass balance constraints and maximizes or minimizes a specific objective function, typically related to cellular growth or production of a particular metabolite[6]. By simulating different conditions and constraints, FBA provides insights into the metabolic capabilities and limitations of the cell.

Another essential aspect of MFA is the integration of kinetic information into the analysis. While traditional MFA often assumes a steady-state condition, actual cellular metabolism is dynamic and subject to various regulatory mechanisms. Incorporating kinetic data, such as enzyme activities and reaction rates, can enhance the accuracy of flux estimations and provide a more comprehensive understanding of metabolic regulation. Advanced MFA techniques, including dynamic MFA, aim to capture these temporal changes and offer a more detailed view of metabolic fluxes in response to environmental

or genetic perturbations[7]. This integration of kinetic data with stoichiometric models represents an evolving frontier in the field of metabolic analysis.

3. Stoichiometric Models

Stoichiometric models are the foundational framework for Metabolic Flux Analysis (MFA). These models represent the metabolic network of an organism as a set of linear equations, each corresponding to a specific biochemical reaction. In these equations, the stoichiometric coefficients denote the number of molecules involved in each reaction, encompassing both reactants and products. By detailing the interconnections between metabolites, stoichiometric models enable the comprehensive mapping of metabolic pathways, allowing researchers to study the flow of metabolites through these pathways systematically[8].

The construction of stoichiometric models begins with the identification and cataloging of all relevant metabolic reactions within a cell. This process often involves extensive literature reviews and database mining to ensure that the model includes all known reactions and metabolites. Genome-scale metabolic reconstructions, which compile all enzymatic reactions encoded by an organism's genome, are frequently used as the basis for these models. These reconstructions provide a detailed blueprint of cellular metabolism, capturing the complexity and interconnectivity of metabolic networks.

A key feature of stoichiometric models is their ability to accommodate constraints, which can reflect various physiological conditions. These constraints include mass balance, thermodynamic feasibility, and capacity limitations of enzymes. Mass balance constraints ensure that the total input and output of metabolites for each reaction are equal, maintaining the conservation of mass. Thermodynamic constraints ensure that the directionality of reactions is consistent with known biochemical principles, while enzyme capacity constraints reflect the maximum rates at which reactions can occur given the available enzyme levels[9]. By incorporating these constraints, stoichiometric models can simulate realistic metabolic scenarios.

Stoichiometric models are integral to various computational techniques used in MFA, such as Flux Balance Analysis (FBA) and elementary mode analysis. In FBA, the stoichiometric model is used to formulate a linear programming problem, where the objective is to find a flux distribution that maximizes or minimizes a specific cellular function, such as biomass production or ATP generation. Elementary mode analysis, on the other hand, identifies all possible minimal sets of reactions that can operate at steady state, providing insights

into the fundamental pathways that support cellular metabolism. These techniques leverage stoichiometric models to predict cellular behavior under different genetic and environmental conditions, guiding metabolic engineering and synthetic biology efforts. The fig.2 represents Stoichiometric modelling of cell metabolism.

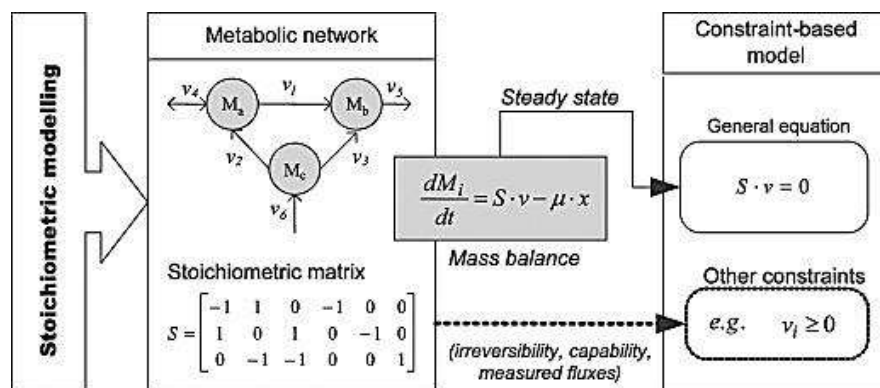


Fig.2: Stoichiometric modelling of cell metabolism

Stoichiometric models also play a crucial role in integrating multi-omics data, such as genomics, transcriptomics, proteomics, and metabolomics. By overlaying these data onto the stoichiometric framework, researchers can gain a holistic view of cellular metabolism and identify key regulatory points. This integrated approach enhances the predictive power of the models and facilitates the design of targeted interventions to optimize metabolic pathways[10]. As experimental technologies and computational methods continue to advance, stoichiometric models will become even more detailed and accurate, driving forward our understanding and manipulation of complex metabolic systems.

4. Flux Balance Analysis (FBA)

Flux Balance Analysis (FBA) is a cornerstone computational method in Metabolic Flux Analysis (MFA) used to predict the flow of metabolites through a metabolic network. FBA operates on the principle of mass conservation, assuming that the cellular system is at a steady state where the concentrations of metabolites remain constant over time. This assumption allows FBA to transform the stoichiometric model of the metabolic network into a system of linear equations[11]. The primary goal of FBA is to find the optimal distribution of metabolic fluxes that satisfy these equations while optimizing a specific objective function, typically related to cellular growth or the production of a particular metabolite. The fig.3 shows the Result of FBA.

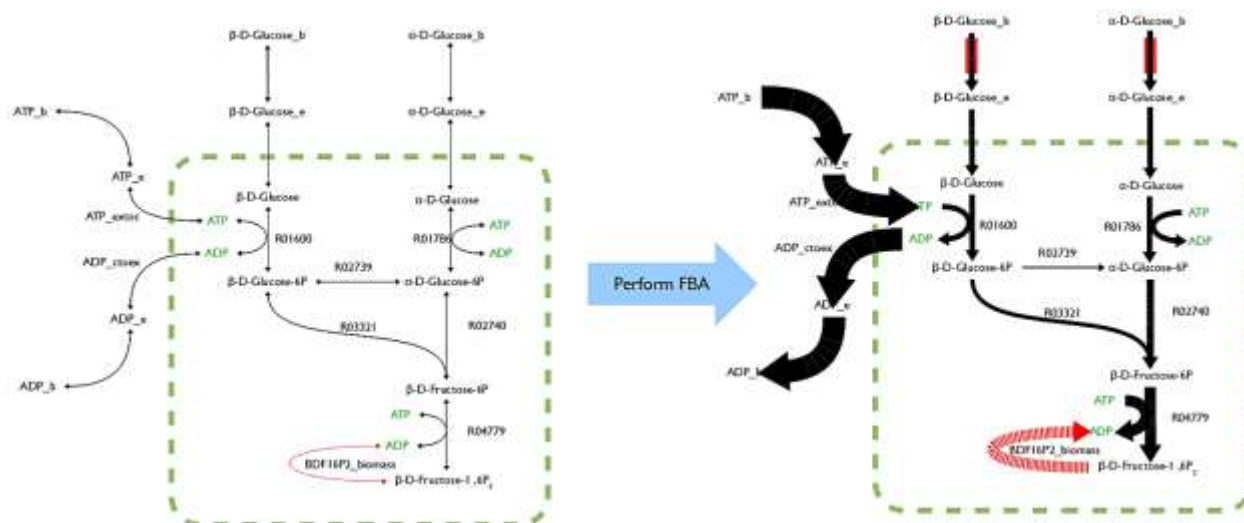


Fig.3: Result of FBA

The results of FBA on a prepared metabolic network of the top six reactions of glycolysis. The predicted flux through each reaction is proportional to the width of the line. Objective function in red, constraints on alpha-D-glucose and beta-D-glucose import represented as red bars.

To perform FBA, researchers first construct a stoichiometric matrix (S-matrix) that captures all the metabolic reactions in the network. Each row of the S-matrix represents a metabolite, and each column represents a reaction, with the entries corresponding to the stoichiometric coefficients. The next step involves defining an objective function, such as maximizing biomass yield or minimizing ATP consumption[12]. This objective function is then subjected to linear programming techniques to solve for the flux distribution that best meets the desired outcome. The result is a set of flux values that indicate the rate at which each reaction occurs, providing a snapshot of the cell's metabolic state under the given conditions.

In Flux Balance Analysis (FBA), the impact of inhibiting a reaction, rather than completely removing it, can be simulated by limiting the permissible flux through that reaction. The effect of this inhibition can be classified as lethal or non-lethal using criteria similar to those applied in the case of reaction deletions. Specifically, a threshold is used to distinguish between "substantially reduced" and "slightly reduced" fluxes. While the choice of this threshold is often arbitrary, a reasonable estimate can be derived from growth experiments where the simulated inhibitions or deletions are implemented and the growth rate is measured[13].

A significant advantage of FBA is its ability to make predictions about cellular behavior in response to genetic and environmental perturbations. By modifying the constraints of the stoichiometric model, such as by knocking out genes or changing nutrient availability, FBA can simulate how these changes affect metabolic fluxes. This capability is particularly valuable in metabolic engineering, where the goal is to optimize microbial strains for the production of biofuels, pharmaceuticals, or other valuable compounds. FBA helps identify potential bottlenecks and suggests genetic modifications to improve production efficiency.

Despite its robustness, FBA has certain limitations, primarily stemming from its reliance on steady-state assumptions and the accuracy of the stoichiometric model. Real cellular systems often exhibit dynamic behaviors and regulatory mechanisms that FBA does not capture[14]. Additionally, the choice of the objective function can significantly influence the results, and determining the most appropriate objective function is not always straightforward. To address these limitations, researchers have developed extensions to FBA, such as dynamic FBA (dFBA) and regulatory FBA (rFBA), which incorporate temporal changes and regulatory constraints, respectively. These advancements aim to enhance the predictive accuracy of FBA and extend its applicability to more complex and realistic biological scenarios.

5. Experimental Techniques in MFA

Experimental techniques in Metabolic Flux Analysis (MFA) are essential for accurately measuring intracellular metabolite concentrations and fluxes, providing the empirical data needed to validate and refine computational models. One of the most widely used techniques is isotopic labeling, which involves incorporating stable isotopes, such as ^{13}C into metabolic substrates. As the labeled substrate is metabolized, the isotopic label is distributed through various metabolic intermediates[15]. By analyzing the distribution of these labels in metabolites, researchers can infer the fluxes through different metabolic pathways. This method provides detailed insights into the dynamic flow of metabolites within cells.

Mass spectrometry (MS) is a critical analytical tool in MFA, enabling the detection and quantification of isotopically labeled metabolites with high sensitivity and precision. MS can identify and measure the abundance of labeled and unlabeled forms of metabolites, allowing for the reconstruction of metabolic fluxes. Techniques such as Gas Chromatography-Mass Spectrometry (GC-MS) and Liquid Chromatography-Mass Spectrometry (LC-MS) are

commonly used to analyze complex mixtures of metabolites[16]. These methods offer high-resolution data on metabolite concentrations, which are crucial for building accurate metabolic models. The fig.4 depicts the Structure of Mass Spectrometry.

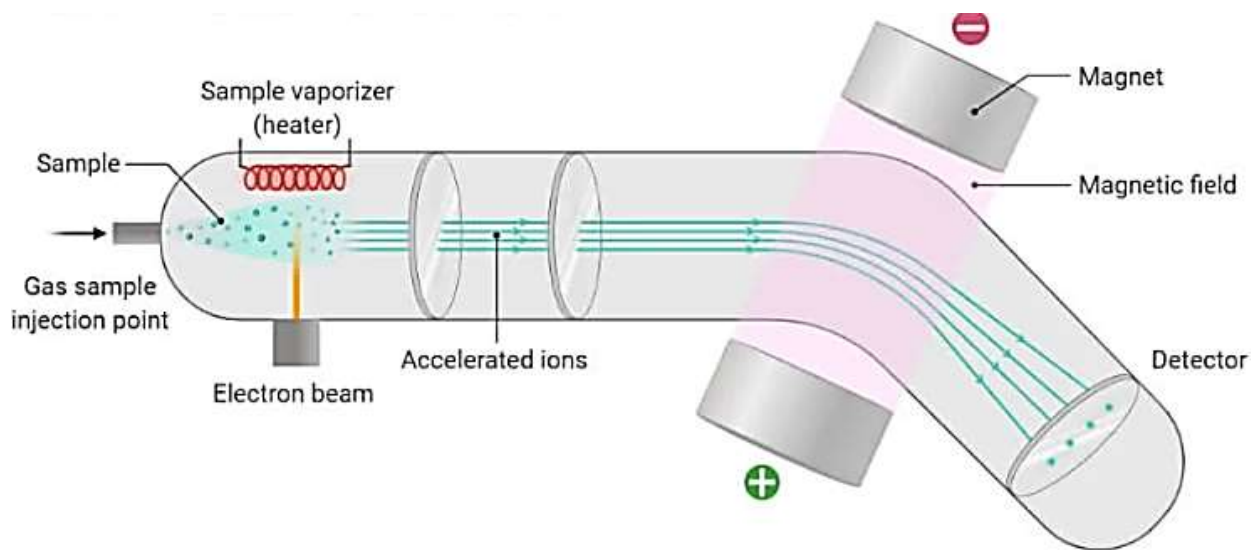


Fig4: Structure of Mass Spectrometry

Nuclear Magnetic Resonance (NMR) spectroscopy is another powerful technique used in MFA. NMR provides detailed information on the structure and concentration of metabolites, as well as the distribution of isotopic labels within them. Unlike MS, which requires extensive sample preparation and can be destructive, NMR is a non-destructive technique that allows for the continuous monitoring of metabolic processes in living cells. This makes NMR particularly valuable for studying dynamic changes in metabolic fluxes over time[17]. Additionally, NMR can be used to measure the flux of metabolites in real-time, providing a comprehensive view of cellular metabolism. The Fig.5 depicts Nuclear Magnetic Resonance (NMR) spectroscopy.

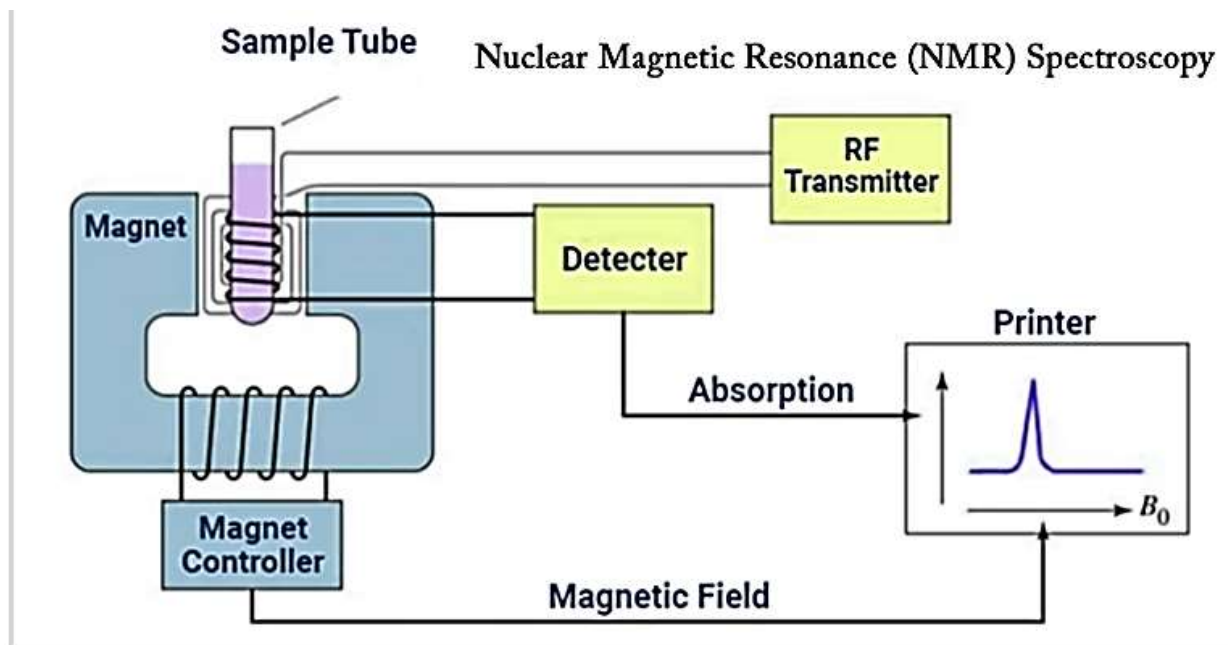


Fig.5: Nuclear Magnetic Resonance (NMR) spectroscopy

Combining these experimental techniques with computational modeling enhances the accuracy and reliability of MFA. By integrating isotopic labeling data with MS and NMR measurements, researchers can construct detailed and robust metabolic models. These models are further validated and refined through iterative cycles of experimentation and computation, leading to a deeper understanding of cellular metabolism. Advances in experimental techniques continue to push the boundaries of MFA, enabling the analysis of more complex and dynamic metabolic systems and paving the way for novel applications in biotechnology and medicine.

6. Applications in Biotechnology

Metabolic Flux Analysis (MFA) has become an indispensable tool in biotechnology, driving advancements in diverse fields such as metabolic engineering, synthetic biology, and drug development. In metabolic engineering, MFA is used to optimize microbial production systems for the efficient synthesis of valuable compounds like biofuels, pharmaceuticals, and industrial chemicals. By mapping the metabolic pathways and identifying bottlenecks or inefficiencies, MFA guides the targeted genetic modifications needed to enhance production yields[18]. For example, MFA has been employed to increase the production of ethanol in yeast and the synthesis of amino acids in bacteria, significantly improving the economic viability of these bioprocesses.

In synthetic biology, MFA aids in the design and construction of novel metabolic pathways for the production of complex natural products and biopharmaceuticals. By providing a quantitative understanding of flux distributions within a cell, MFA helps synthetic biologists engineer pathways that efficiently channel metabolites towards the desired end products. This approach has been applied to create microbial factories capable of producing rare or difficult-to-synthesize compounds, such as artemisinin, a key anti-malarial drug. The ability to predict and control metabolic fluxes through synthetic pathways enables the development of more robust and efficient production systems.

Drug development also benefits significantly from MFA, particularly in understanding the metabolic effects of new drug candidates. By analyzing how drugs influence cellular metabolism, MFA can identify potential metabolic targets and predict off-target effects, thereby enhancing the efficacy and safety of new therapeutics. Additionally, MFA is crucial in cancer research, where it helps elucidate the altered metabolic states of cancer cells. Understanding the unique metabolic dependencies of cancer cells can lead to the development of targeted therapies that disrupt these pathways, offering new strategies for cancer treatment[19].

Environmental biotechnology is another area where MFA has considerable impact. It is used to optimize microbial processes for waste treatment and bioremediation, improving the efficiency of pollutant degradation and bioenergy production from waste materials. By analyzing the metabolic fluxes in microbial communities involved in these processes, MFA helps identify key metabolic pathways and interactions that can be manipulated to enhance performance. For instance, MFA has been applied to improve the degradation of toxic compounds in contaminated environments and to optimize the production of biogas from organic waste. These applications not only address environmental challenges but also contribute to the development of sustainable and renewable bio-based technologies.

7. Challenges and Considerations

Despite its transformative potential, Metabolic Flux Analysis (MFA) faces several challenges that researchers must navigate to fully exploit its capabilities. One of the primary challenges is the accuracy and completeness of the stoichiometric models used in MFA. These models are based on known metabolic reactions and pathways, but gaps in knowledge and incomplete metabolic reconstructions can lead to inaccuracies in flux predictions.

Ensuring that models are comprehensive and up-to-date requires continuous efforts in metabolic research, genome annotation, and data integration, as well as leveraging advanced techniques such as genome-scale metabolic reconstructions[20]. Another significant challenge in MFA is the measurement of intracellular fluxes. While techniques like isotopic labeling, mass spectrometry, and NMR spectroscopy provide valuable data, they also have limitations in sensitivity, resolution, and the ability to capture dynamic changes in metabolism. Accurate flux estimation often relies on steady-state assumptions, which may not always hold true in biological systems that exhibit transient or oscillatory behaviors. Developing methods to measure fluxes in real-time and under non-steady-state conditions remains an active area of research, aiming to provide a more realistic depiction of cellular metabolism. The integration of multi-omics data, such as genomics, transcriptomics, proteomics, and metabolomics, into MFA presents both opportunities and challenges. While this integrated approach can enhance the accuracy and predictive power of metabolic models, it also requires sophisticated computational tools and algorithms to manage and analyze large datasets. Additionally, discrepancies between different types of omics data can complicate the interpretation of results. Addressing these challenges involves developing robust computational frameworks and standardizing data collection and analysis protocols to ensure consistency and reliability across studies. Regulatory and kinetic complexities of cellular metabolism pose additional hurdles for MFA. Traditional MFA approaches often do not account for the regulatory mechanisms and enzyme kinetics that control metabolic fluxes. Cellular metabolism is highly regulated by factors such as enzyme levels, post-translational modifications, and allosteric interactions, which can significantly influence flux distributions. Incorporating these regulatory elements into MFA models requires advanced techniques such as dynamic MFA and regulatory FBA, which aim to capture the temporal and regulatory dynamics of metabolism. Balancing model complexity with computational feasibility is crucial for accurately predicting metabolic behaviors under various conditions[21].

Lastly, the application of MFA in biotechnology also involves practical considerations related to experimental design and validation. Ensuring that experimental conditions accurately reflect the physiological state of the cells under study is essential for meaningful flux analysis. Additionally, validating computational predictions through independent experiments is critical for confirming the reliability and applicability of MFA findings. This iterative process of modeling, experimentation, and validation is fundamental to

advancing the field and translating MFA insights into practical biotechnological solutions.

8. Future Direction

The future of Metabolic Flux Analysis (MFA) holds great promise as advancements in both experimental techniques and computational modeling continue to evolve. One significant direction is the integration of real-time flux analysis. Current MFA methods often rely on steady-state assumptions, but the development of dynamic MFA approaches aims to capture the temporal changes in metabolic fluxes. Real-time analysis would enable a more accurate representation of cellular metabolism under various physiological conditions, enhancing our understanding of metabolic responses to environmental fluctuations, genetic modifications, and drug treatments[22].

Another promising direction is the expansion of MFA to more complex biological systems, such as multicellular organisms and microbial consortia. Traditionally, MFA has been applied predominantly to single-cell systems like bacteria and yeast. However, extending these techniques to multicellular organisms can provide insights into tissue-specific metabolism, intercellular metabolic interactions, and overall organismal physiology. Similarly, studying microbial communities using MFA can uncover the metabolic interdependencies and synergies that drive community behavior and function, which is particularly relevant for applications in environmental biotechnology and human health.

The integration of multi-omics data into MFA is expected to become more sophisticated, providing a more comprehensive view of cellular metabolism. Advances in high-throughput sequencing, proteomics, and metabolomics will generate vast amounts of data that can be incorporated into MFA models. This integrated approach will enable the construction of more accurate and detailed metabolic networks, improving the predictive power of MFA. Moreover, the development of new computational tools and algorithms to handle and analyze these large datasets will be crucial for advancing the field. Machine learning and artificial intelligence (AI) are also poised to revolutionize MFA. By leveraging machine learning algorithms, researchers can identify patterns and relationships within complex metabolic data that may not be apparent through traditional methods. AI can assist in optimizing metabolic pathways, predicting the effects of genetic modifications, and designing novel metabolic networks for synthetic biology applications. The combination of AI with MFA has the potential to accelerate the discovery of new metabolic engineering strategies

and enhance the efficiency of biotechnological processes[23]. Lastly, the application of MFA in personalized medicine represents a transformative future direction. By analyzing the metabolic profiles of individual patients, MFA can help identify unique metabolic biomarkers and therapeutic targets. This personalized approach can lead to the development of tailored treatments that are more effective and have fewer side effects. For example, in cancer therapy, understanding the specific metabolic alterations in a patient's tumor can guide the selection of targeted treatments that exploit the tumor's metabolic vulnerabilities. As the field of MFA continues to advance, its integration into clinical practice could significantly improve the diagnosis, treatment, and management of various diseases[24].

9. Conclusion

Metabolic Flux Analysis (MFA) has established itself as a pivotal tool in biotechnology, offering profound insights into cellular metabolism and facilitating advancements in metabolic engineering, synthetic biology, drug development, and environmental biotechnology. Through the construction of stoichiometric models and the application of sophisticated experimental and computational techniques, MFA enables the detailed mapping and optimization of metabolic pathways. Despite challenges such as the accuracy of stoichiometric models, the integration of multi-omics data, and the need for dynamic flux analysis, ongoing advancements promise to enhance the precision and applicability of MFA. As we look to the future, the incorporation of real-time analysis, machine learning, and personalized medicine holds the potential to further revolutionize the field, driving innovation and improving outcomes in both industrial and clinical settings. The continued evolution of MFA will undoubtedly unlock new possibilities for understanding and manipulating complex metabolic networks, solidifying its role as a cornerstone of modern biotechnology.

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