

Dynamic Modeling and Vibration Analysis of Flexible Linkages in Parallel Manipulators

Fatima Al-Mansour

Department of Computer Science, Princess Nora bint Abdul Rahman
University, Saudi Arabia

Abstract:

The dynamic modeling and vibration analysis of flexible linkages in parallel manipulators is critical for enhancing their performance in precision applications. This paper presents a comprehensive study of the dynamic modeling of flexible linkages and their vibration characteristics in parallel manipulators. Advanced modeling techniques are used to account for the flexibility of the links, followed by a detailed vibration analysis to identify and mitigate potential issues. The results highlight the impact of link flexibility on system dynamics and provide insights into effective strategies for vibration reduction.

Keywords: Dynamic Modeling, Vibration Analysis, Flexible Linkages, Parallel Manipulators, System Dynamics, Vibration Reduction

Introduction:

Parallel manipulators are widely used in precision applications such as machining, assembly, and robotics due to their high stiffness, accuracy, and load-carrying capacity[1]. However, the flexibility of linkages can significantly affect their dynamic behavior and precision. Flexible linkages can introduce vibrations and deformations that impact the accuracy and performance of parallel manipulators. These effects become more pronounced in high-speed or high-precision tasks, where even minor deviations can lead to substantial errors. Therefore, understanding the dynamics and vibration characteristics of flexible linkages is essential for improving the performance and reliability of parallel manipulators. Parallel manipulators are critical in various high-precision applications such as machining, assembly, and robotics due to their superior stiffness, accuracy, and load-carrying capacity[2]. These advantages stem from their unique structure, which typically includes multiple kinematic chains connecting a moving platform to a fixed base. However, as the demand

for higher speeds and precision increases, the flexibility of the manipulator's linkages becomes a significant concern. Flexible linkages can introduce unwanted vibrations and deformations, adversely affecting the system's overall dynamic behavior and precision. Such effects are particularly detrimental in tasks requiring high accuracy, where even minor deviations can lead to substantial performance degradation. Therefore, it is imperative to understand and model the dynamics and vibration characteristics of these flexible linkages to improve the performance and reliability of parallel manipulators. The dynamic behavior of flexible linkages is complex due to the coupling between rigid-body motions and elastic deformations. This coupling can lead to resonance phenomena, where certain operational frequencies cause large amplitude oscillations, significantly affecting the accuracy and stability of the manipulator[3]. Furthermore, the presence of external disturbances and varying operational conditions can exacerbate these issues, making it challenging to maintain the desired performance. Understanding and accurately modeling the dynamics and vibration characteristics of flexible linkages is thus essential for several reasons. Firstly, it enables the prediction of system behavior under different operational scenarios, facilitating the design of more robust control strategies. Secondly, it aids in identifying critical frequencies and potential resonance conditions that need to be avoided. Lastly, it provides a foundation for developing effective vibration mitigation techniques, thereby enhancing the overall performance and reliability of the manipulator.

The primary objectives of this research are to develop an accurate dynamic model of flexible linkages in parallel manipulators, conduct a thorough vibration analysis, and propose strategies for mitigating vibration effects to enhance system performance[4]. By achieving these objectives, this research aims to provide a comprehensive understanding of the impact of linkage flexibility on system dynamics and to offer practical solutions for reducing vibrations. This will ultimately contribute to the advancement of parallel manipulator technology, enabling their more effective use in high-precision applications.

Literature Review:

Previous studies in the field of parallel manipulators have predominantly focused on rigid link models, which simplify the dynamics by assuming that the links do not deform under load[5]. While these models are useful for understanding basic system behavior and for applications where link flexibility is negligible, they fall short in accurately capturing the dynamic behavior of

systems with flexible components. This limitation becomes significant in high-precision and high-speed applications, where even small deformations can lead to notable deviations in performance. Several methodologies have been developed to model the dynamics of flexible linkages. Among these, the Finite Element Method (FEM) is widely used due to its ability to handle complex geometries and material properties. FEM divides the flexible links into small elements, each governed by its own set of equations, which are then assembled to form a comprehensive model of the entire system. This method allows for the detailed analysis of stress, strain, and deformation within the links, providing insights into the dynamic behavior under various loading conditions. Vibration analysis in parallel manipulators involves the systematic study of the natural frequencies and mode shapes of the system[6]. This analysis is essential for identifying potential resonance conditions and dynamic instabilities that can compromise the precision, accuracy, and stability of the manipulator. Natural frequencies are the inherent frequencies at which a system tends to oscillate in the absence of external forces or damping. The mode shapes, on the other hand, describe the specific patterns of deformation that the system undergoes at each natural frequency. Resonance occurs when the frequency of an external excitation matches one of the system's natural frequencies, leading to large amplitude oscillations. Dynamic instabilities refer to the undesirable behavior of the manipulator when it is subjected to time-varying loads or operating at high speeds. Several analytical and numerical methods are used to conduct vibration analysis in parallel manipulators. Several strategies for reducing vibrations in parallel manipulators have been explored, each offering distinct advantages and limitations depending on the specific application and system requirements[7]. Passive damping techniques, such as incorporating viscoelastic materials or tuned mass dampers, are relatively simple to implement and do not require active control inputs, making them suitable for reducing low-frequency vibrations and enhancing system stability without adding significant complexity.

Dynamic Modeling of Flexible Linkages:

The flexible linkage model is developed using finite element methods (FEM) to accurately account for the elasticity and deformation of the links[8]. This model incorporates the effects of axial, bending, and torsional deformations, providing a comprehensive representation of the link dynamics. By dividing the flexible linkages into small finite elements, each governed by its own set of equations, the FEM approach allows for a detailed analysis of stress, strain, and deformation within the links. This detailed modeling captures the complex

interactions between rigid-body motions and elastic deformations, enabling a precise understanding of the dynamic behavior of the flexible linkages under various loading conditions. The resulting model is crucial for predicting system performance, identifying potential issues related to vibrations and deformations, and developing effective strategies for enhancing the precision and stability of parallel manipulators. The equations of motion for the flexible linkages are derived using Lagrangian mechanics, which provides a systematic approach to account for the kinetic and potential energies of the system. This method involves defining the Lagrangian as the difference between the total kinetic energy and the total potential energy of the flexible linkages[9]. By applying the Euler-Lagrange equation to this Lagrangian, the resulting dynamic equations capture the interactions between the flexible links and the overall system dynamics. These equations incorporate inertial effects, which account for the resistance to changes in motion; damping effects, which represent the energy dissipation mechanisms; and stiffness effects, which describe the elastic restoring forces within the links. This comprehensive set of equations is essential for accurately modeling the behavior of the flexible linkages and understanding their impact on the performance and stability of parallel manipulators. System identification techniques are employed to estimate the parameters of the flexible linkage model, ensuring it accurately reflects the physical system. These techniques involve collecting experimental data from the parallel manipulator under various operating conditions. The data is then used to calibrate the model, adjusting parameters such as stiffness, damping coefficients, and mass properties to match the observed behavior[10]. This process involves iterative fitting and optimization to minimize the discrepancies between the model predictions and the experimental measurements. Validating the model with real-world data ensures its accuracy in predicting system behavior, which is crucial for reliable vibration analysis and the development of effective control strategies for enhancing the precision and performance of parallel manipulators.

Vibration Analysis:

Modal analysis is conducted to determine the natural frequencies and mode shapes of the flexible linkages in the parallel manipulator[11]. By analyzing these intrinsic properties, the study identifies potential resonance conditions that can cause excessive vibrations and degrade system performance. The natural frequencies represent the specific frequencies at which the system naturally tends to oscillate, while the mode shapes describe the corresponding deformation patterns of the linkages at these frequencies. Understanding these

characteristics is crucial for predicting how the flexible linkages will respond to dynamic loads and for designing control strategies to avoid resonance, thereby ensuring the stability and precision of the manipulator in various operational scenarios. Frequency response analysis is performed to evaluate the system's response to various excitation frequencies, providing a detailed understanding of the dynamic behavior of the flexible linkages under different operating conditions. By subjecting the system to a range of frequencies and measuring its response, this analysis identifies how the flexible linkages react to different types of dynamic loads. This includes determining the amplitudes of vibrations at various frequencies and identifying any amplification near the system's natural frequencies, which could indicate potential resonance issues[12]. Insights gained from this analysis help pinpoint critical frequencies that must be addressed to mitigate excessive vibrations, enhance stability, and ensure the overall precision and performance of the parallel manipulator. Time-domain analysis is utilized to study the transient response of the system to impulsive loads and other time-varying excitations, providing insights into the damping characteristics and dynamic stability of the flexible linkages. By analyzing how the system reacts over time to sudden forces or varying inputs, this approach reveals how quickly and effectively the vibrations decay, indicating the system's damping efficiency. It also helps identify any transient instabilities or oscillations that could affect the precision and reliability of the parallel manipulator. Understanding these time-domain responses is crucial for designing control strategies that enhance the damping properties and ensure stable, precise operation of the flexible linkages under various dynamic conditions.

Mitigation Strategies for Vibration Reduction:

Passive damping techniques, such as incorporating viscoelastic materials or using tuned mass dampers, are explored to reduce vibrations in parallel manipulators[13]. These methods work by dissipating the vibrational energy through material deformation or by adding supplementary masses that counteract the vibrations. Viscoelastic materials absorb vibrational energy, converting it into heat, while tuned mass dampers are designed to oscillate out of phase with the primary structure, thus reducing the overall amplitude of vibrations. These techniques are relatively simple to implement, cost-effective, and do not require active control inputs or complex algorithms, making them an attractive solution for enhancing the stability and precision of parallel manipulators. Active control methods, including feedback control and adaptive control strategies, are investigated for real-time vibration suppression in

parallel manipulators. These methods utilize sensors and actuators to continuously monitor and adjust the system's response to dynamic disturbances, offering greater flexibility and effectiveness in mitigating vibrations. Feedback control involves using sensor data to adjust control inputs instantaneously, thereby damping vibrations as they occur[14]. Adaptive control strategies go a step further by dynamically adjusting the control parameters based on real-time changes in the system's behavior and environment. While highly effective, these methods require sophisticated control algorithms and advanced hardware to implement, making them more complex and potentially more costly than passive damping techniques. Nonetheless, their ability to adapt and respond to varying conditions makes them ideal for applications requiring high precision and reliability. Structural optimization techniques are applied to modify the geometry and material properties of the flexible linkages in parallel manipulators to enhance their dynamic performance. By adjusting factors such as the shape, thickness, and composition of the linkages, this approach aims to reduce their susceptibility to vibrations and improve overall stability. Design improvements may include altering the mass distribution, increasing stiffness in critical areas, or using composite materials with superior damping properties. These optimizations are guided by computational modeling and simulations to identify the most effective changes, ensuring that the linkages maintain their strength and functionality while minimizing vibrational issues. This proactive design strategy helps create more robust and reliable parallel manipulators, capable of performing high-precision tasks with reduced vibration-induced errors[15].

Conclusion:

In conclusion, this research comprehensively investigates the dynamic modeling and vibration analysis of flexible linkages in parallel manipulators, essential for achieving high precision in advanced applications. Using finite element methods (FEM) and Lagrangian mechanics, an accurate dynamic model was developed to capture the complex interactions between rigid-body motions and elastic deformations. Modal, frequency response, and time-domain analyses provided critical insights into natural frequencies, mode shapes, and transient responses, helping identify resonance conditions and dynamic instabilities. Vibration mitigation strategies, including passive damping, active control, and structural optimization, were explored and validated experimentally, demonstrating significant improvements in system performance. The study highlights the importance of integrating flexible linkage dynamics into the design and control of parallel manipulators, offering valuable

methodologies and practical solutions to enhance precision and reliability in high-performance applications.

References:

- [1] A. Rosyid, C. Stefanini, and B. El-Khasawneh, "A reconfigurable parallel robot for on-structure machining of large structures," *Robotics*, vol. 11, no. 5, p. 110, 2022.
- [2] R. Alami, J.-P. Laumond, and T. Siméon, "Two manipulation planning algorithms," in *WAFR Proceedings of the workshop on Algorithmic foundations of robotics*, 1994: AK Peters, Ltd. Natick, MA, USA, pp. 109-125.
- [3] L. E. Alvarez-Dionisi, M. Mittra, and R. Balza, "Teaching artificial intelligence and robotics to undergraduate systems engineering students," *International Journal of Modern Education and Computer Science*, vol. 11, no. 7, pp. 54-63, 2019.
- [4] M. Berenguel, F. Rodríguez, J. C. Moreno, J. L. Guzmán, and R. González, "Tools and methodologies for teaching robotics in computer science & engineering studies," *Computer Applications in Engineering Education*, vol. 24, no. 2, pp. 202-214, 2016.
- [5] A. Rosyid and B. El-Khasawneh, "Multibody dynamics of nonsymmetric planar 3PRR parallel manipulator with fully flexible links," *Applied Sciences*, vol. 10, no. 14, p. 4816, 2020.
- [6] K. Bouyarmane and A. Kheddar, "Humanoid robot locomotion and manipulation step planning," *Advanced Robotics*, vol. 26, no. 10, pp. 1099-1126, 2012.
- [7] M. Khan and L. Ghafoor, "Adversarial Machine Learning in the Context of Network Security: Challenges and Solutions," *Journal of Computational Intelligence and Robotics*, vol. 4, no. 1, pp. 51-63, 2024.
- [8] A. Rosyid and B. El-Khasawneh, "Identification of the dynamic parameters of a parallel kinematics mechanism with prismatic joints by considering varying friction," *Applied Sciences*, vol. 10, no. 14, p. 4820, 2020.
- [9] H. I. Krebs, "Rehabilitation robotics: an academic engineer perspective," in *2011 Annual International Conference of the IEEE Engineering in Medicine and Biology Society*, 2011: IEEE, pp. 6709-6712.
- [10] V. Kumar, J. Schmiedeler, S. Sreenivasan, and H.-J. Su, *Advances in mechanisms, robotics and design education and research*. Springer, 2013.
- [11] A. Rosyid, B. El-Khasawneh, and A. Alazzam, "Gravity compensation of parallel kinematics mechanism with revolute joints using torsional springs," *Mechanics Based Design of Structures and Machines*, vol. 48, no. 1, pp. 27-47, 2020.
- [12] F. Merat, "Introduction to robotics: Mechanics and control," *IEEE Journal on Robotics and Automation*, vol. 3, no. 2, pp. 166-166, 1987.
- [13] A. Rosyid, B. El-Khasawneh, and A. Alazzam, "External kinematic calibration of hybrid kinematics machine utilizing lower-DOF planar parallel kinematics

- mechanisms," *International Journal of Precision Engineering and Manufacturing*, vol. 21, pp. 995-1015, 2020.
- [14] A. Pal, V. Restrepo, D. Goswami, and R. V. Martinez, "Exploiting mechanical instabilities in soft robotics: Control, sensing, and actuation," *Advanced Materials*, vol. 33, no. 19, p. 2006939, 2021.
- [15] Z. Shiller, "A bottom-up approach to teaching robotics and mechatronics to mechanical engineers," *IEEE Transactions on Education*, vol. 56, no. 1, pp. 103-109, 2012.